

Special Cases

Warm UP → One more new idea!

Key



Two problems:

a. $3 - 6(x - 5) = 5x$

$$3 - 6x + 30 = 5x$$

$$-6x + 30 = 5x$$

$$30 = 11x$$

$$\boxed{3 = x}$$

b. $3x + 8 - 5x = 10 - 5x$

$$-2x + 8 = 10 - 5x$$

$$3x = 2$$

$$\boxed{x = \frac{2}{3}}$$

Two more.....hmmmm:

a. $5(z - 8) = -40 + 5z$

$$5z - 40 = -40 + 5z$$

$$0 = 0$$

TRUE

b. $2x + 7 - 4x = 5 - \frac{1}{2}(4x - 8)$

$$-2x + 7 = 5 - 2x + 4$$

$$-2x + 7 = 9 - 2x$$

$7 \neq 9$ FALSE

(IM5) infinitely many solutions

SOOOOO..... If we end up with a true statement then our answer is all real #'s \mathbb{R}

And if we end up with a false statement then we have no real solutions

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Two more.....hmmmm:

a. $5(z - 8) = -40 + 5z$

b. $2x + 7 - 4x = 5 - \frac{1}{2}(4x - 8)$

SOOOOO..... If we end up with a _____ statement then our answer is _____

And if we end up with a _____ then we have _____

A few practice problems:

$$1) 2(k - 1) = -\frac{1}{2}(-4k + 4)$$

$$2k - 2 = 2k - 2$$

$$0 = 0$$

all real #s

$$2) 5(1 + 4s) = 2(3 + 10s)$$

$$5 + 20s = 6 + 20s$$

$$5 \neq 6$$

no solution

$$3) \frac{x}{2} - 5 = -7 + 2$$

$$\frac{x}{2} - 5 = -5$$

$$\frac{x}{2} = 0$$

x = 0

$$4) 10 - 2(x + 4) = 8 - 4x$$

$$10 - 2x - 8 = 8 - 4x$$

$$-2x + 2 = 8 - 4x$$

$$2x = 6$$

x = 3

A few practice problems:

$$1) 2(k - 1) = -\frac{1}{2}(-4k + 4)$$

$$2) 5(1 + 4s) = 2(3 + 10s)$$

$$3) \frac{x}{2} - 5 = -7 + 2$$

$$4) 10 - 2(x + 4) = 8 - 4x$$