



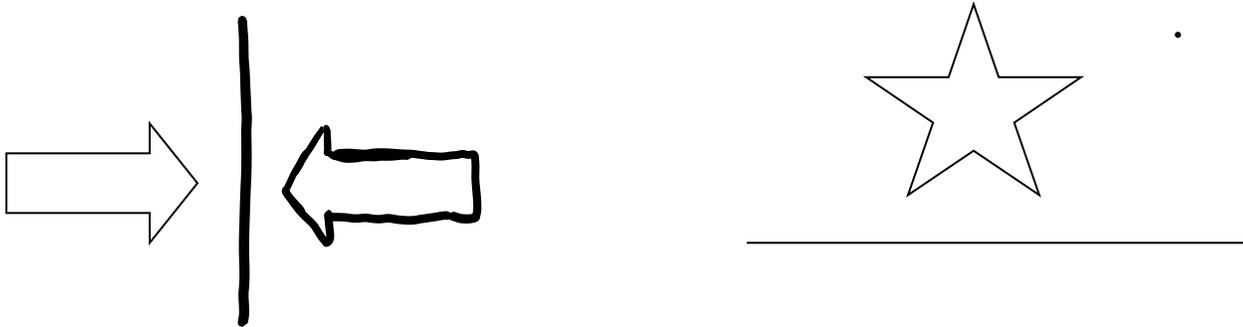
# REFLECTIONS

DAY 1

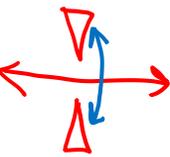


To 'reflect' a graph means to draw its mirror image across a line of symmetry.

Examples: Draw the reflection of the given figures across the line of symmetry.



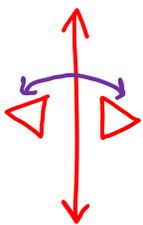
There are two ways to that we will reflect graphs on a coordinate plane.



1) Across the X axis. This means we will be changing the Y values by taking their opposite.

The notation will look like this:  $\downarrow f(x)$  *negative is out front*

Other examples:  $\downarrow -x^2$ ;  $\downarrow -|x|$ ; etc.



2) Across the Y axis. This means we will be changing the X values by taking their opposite.

The notation will look like this:  $f(\downarrow -x)$  *negative is inside the parentheses or bars*

Other examples:  $\downarrow (-x)^2$ ;  $\downarrow |-x|$ ; etc.

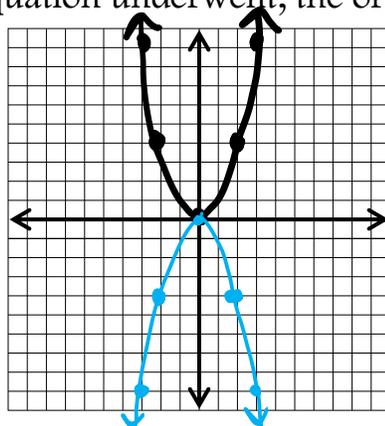
Practice makes perfect ... For each of the following graphs, you have been given  $f(x)$ . List the transformation that the new equation underwent, the original points, and the new points.

1)  $f(x) = x^2$

New Equation:  $-f(x) = \downarrow -x^2$

Transformation:

*- reflection over x  
- take opposite of y*



Original Points:

- $(0, 0)$
- $(-2, 4)$
- $(2, 4)$
- $(-3, 9)$
- $(3, 9)$

New Points:

- $(0, 0)$
- $(-2, -4)$
- $(2, -4)$
- $(-3, -9)$
- $(3, -9)$

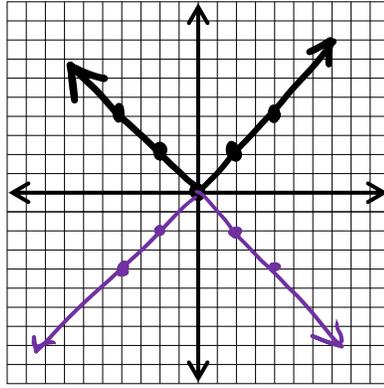
*↑ opposite*

2)  $f(x) = |x|$

New Equation:  $-f(x) = -|x|$

Transformation:

- reflection over x
- opposite of y



Original Points:

- (0, 0)
- (-2, 2)
- (-4, 4)
- (2, 2)
- (4, 4)

↑ opposite

New Points:

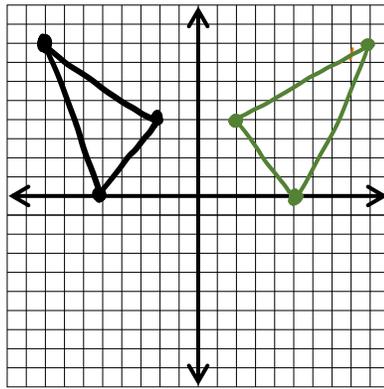
- (0, 0)
- (-2, -2)
- (-4, -4)
- (2, -2)
- (4, -4)

3) Original Equation:  $f(x)$

New Equation:  $f(-x)$

Transformation:

- reflection over y
- opposite of x



Original Points:

- (-5, 0)
- (-2, 4)
- (-8, 8)

↑ opposite

New Points:

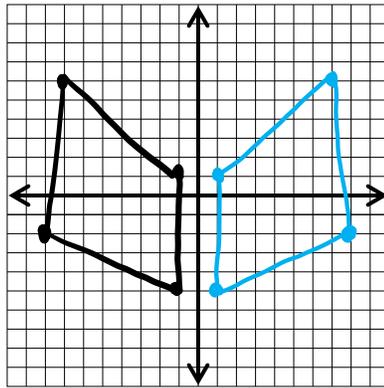
- (5, 0)
- (2, 4)
- (8, 8)

4) Original Equation:  $f(x)$

New Equation:  $f(\frac{1}{x})$

Transformation:

- reflection over y
- opposite of x



Original Points:

- (-8, -2)
- (-7, 6)
- (-1, 1)
- (-1, -5)

↑ opp.

New Points:

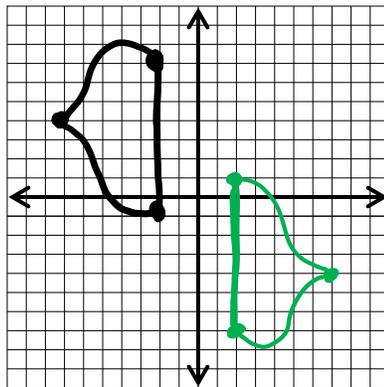
- (8, -2)
- (7, 6)
- (1, 1)
- (1, -5)

5) Original Equation:  $f(x)$

New Equation:  $\frac{1}{f(-x)}$

Transformations:

- reflection over x and y
- opposite of y and x



Original Points:

- (-2, -1)
- (-7, 4)
- (-2, 7)

↑ opp    ↓ opp

New Points:

- (2, 1)
- (7, -4)
- (2, -7)