

Section 5.6Quadratic Formula and the Discriminant

Solve the following equations:

1.  $x^2 - 4 = 0$

$$(x-4)(x+4) = 0$$

$$x = 4, -4$$

2.  $x^2 + 2x = 15$

$$x^2 + 2x - 15 = 0$$

$$(x+5)(x-3) = 0$$

$$x = -5, 3$$

3.  $x^2 - 4x + 8 = 0$  *can't factor!*

$$x = \frac{4 \pm \sqrt{(-4)^2 - 4(1)(8)}}{2(1)} = \frac{4 \pm \sqrt{-16}}{2}$$

$$\frac{4 \pm 4i}{2} = \boxed{2 \pm 2i}$$

What if you can't factor to solve the equation?

<p><b>Quadratic Formula:</b> <math>x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}</math></p>
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Solve the following quadratic equations over the set of complex numbers.

1)  $x^2 - 6x + 73 = 0$

$$x = \frac{6 \pm \sqrt{(-6)^2 - 4(1)(73)}}{2(1)}$$

$$= \frac{6 \pm \sqrt{-256}}{2}$$

$$= \frac{6 \pm 16i}{2} = \boxed{3 \pm 8i} \text{ imaginary}$$

2.  $x^2 - 14x + 50 = 0$

$$x = \frac{14 \pm \sqrt{(-14)^2 - 4(1)(50)}}{2(1)}$$

$$= \frac{14 \pm \sqrt{-4}}{2}$$

$$= \frac{14 \pm 2i}{2} = \boxed{7 \pm i} \text{ imaginary}$$

3.  $x^2 + 2x + 65 = 0$

$$x = \frac{-2 \pm \sqrt{2^2 - 4(1)(65)}}{2(1)}$$

$$= \frac{-2 \pm \sqrt{-256}}{2}$$

$$= \frac{-2 \pm 16i}{2} = \boxed{-1 \pm 8i} \text{ imaginary}$$

4.  $4x^2 - 21x - 18 = 0$

$$x = \frac{21 \pm \sqrt{(-21)^2 - 4(4)(-18)}}{2(4)}$$

$$x = \frac{21 \pm \sqrt{729}}{8}$$

$$= \frac{21 \pm 27}{8} \rightarrow \frac{21+27}{8} = \boxed{6} \text{ 2 real solutions}$$

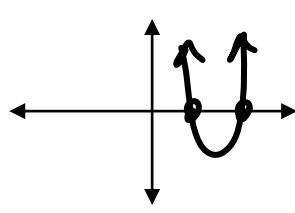
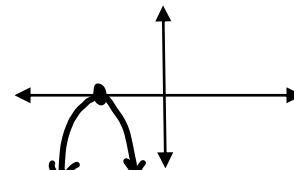
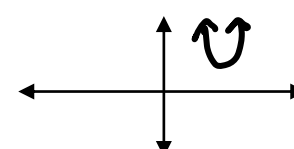
$$\rightarrow \frac{21-27}{8} = \frac{-6}{8} = \boxed{\frac{-3}{4}}$$

## The Discriminant

What is the discriminant and how does it help?

$$b^2 - 4ac$$

\* it tells you the # and type of solutions

Discriminant	# and Type of Roots	Sketch (x-intercepts)
$b^2 - 4ac > 0$ & is a <u>perfect square</u>	2 roots real, rational * factor *	
$b^2 - 4ac > 0$ & is not a perfect square	2 roots real, irrational	
$b^2 - 4ac = 0$	1 root (VERTEX) real, rational	
$b^2 - 4ac < 0$	2 imaginary roots	

Find the value of the discriminant, describe how many and what type of roots and solve for x using the Quadratic Formula.

1.  $x^2 + 8x + 15 = 0$

$$8^2 - 4(1)(15)$$

$$64 - 60$$

$$d = \boxed{4} \text{ * perfect square}$$

2 roots,  
real, rational

2.  $x^2 + 4x - 3 = 0$

$$4^2 - 4(1)(-3)$$

$$16 + 12$$

$$d = \boxed{28}$$

2 roots,  
real, irrational

3.  $4x^2 - 12x + 9 = 0$

$$(-12)^2 - 4(4)(9)$$

$$144 - 144$$

$$d = \boxed{0}$$

1 root  
real, rational  
(VERTEX)

4.  $x^2 - 2x + 8 = 0$

$$(-2)^2 - 4(1)(8)$$

$$4 - 32$$

$$d = \boxed{-28}$$

2 roots,  
imaginary